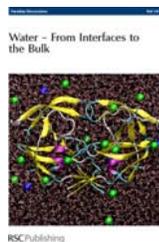


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What ice can teach us about water interactions: a critical comparison of the performance of different water models

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The performance of several popular water models (TIP3P, TIP4P, TIP5P and TIP4P/2005) is analyzed. For that purpose the predictions for ten different properties of water are investigated, namely: 1. vapour–liquid equilibria (VLE) and critical temperature; 2. surface tension; 3. densities of the different solid structures of water (ices); 4. phase diagram; 5. melting-point properties; 6. maximum in the density of water at room pressure and thermal coefficients α and κ_T ; 7. structure of liquid water and ice; 8. equation of state at high pressures; 9. self-diffusion coefficient; 10. dielectric constant. For each property, the performance of each model is analyzed in detail with a critical discussion of the possible reason of the success or failure of the model. A final judgement on the quality of these models is provided. TIP4P/2005 provides the best description of almost all properties of the list, the only exception being the dielectric constant. In second position, TIP5P and TIP4P yield a similar performance overall, and the last place with the poorest description of the water properties is provided by TIP3P. The ideas leading to the proposal and design of the TIP4P/2005 are also discussed in detail. TIP4P/2005 is probably close to the best description of water that can be achieved with a non-polarizable model described by a single Lennard-Jones (LJ) site and three charges.

I. Introduction

Water is probably the most important molecule in our relation to nature. It forms the matrix of life,¹ it is the most common solvent for chemical processes, it plays a major role in the determination of the climate on earth, and it also appears on planets, moons and comets.² Water is interesting not only from a practical point of view, but also from a fundamental point of view. In the liquid phase water presents a number of anomalies when compared to other liquids.^{3–7} In the solid phase it exhibits one of the most complex phase diagrams, having fifteen different solid structures.³ Due to its importance and its complexity, understanding the properties of water from a molecular point of view is of considerable interest. The experimental study of the phase diagram of water has spanned the entire 20th century, starting with the pioneering works of Tammann⁸ and Bridgman⁹ up to the recent discovery of ices XII, XIII and XIV.^{10,11} The existence of several types of amorphous phase at low temperatures,^{12–14} the possible existence of a liquid–liquid phase transition in water,^{15,16} the properties of ice at a free surface^{17–23} and the interaction with hydrophobic molecules^{24,25} have also been the focus of much interest in the last two decades.

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Computer simulations of water started their road with the pioneering papers by Watts and Barker²⁶ and by Rahman and Stillinger²⁷ about forty years ago. A key issue when performing simulations of water is the choice of the potential model used to describe the interaction between molecules.^{28–32} A number of different potential models have been proposed. An excellent survey of the predictions of the different models proposed up to 2002 was made by Guillot.³³ Probably the general feeling is that no water potential model is totally satisfactory and that there are no significant differences between water models.

In the recent years the increase in computing power has allowed the calculation of new properties which can be used as new target quantities in the fit of the potential parameters. More importantly, some of these properties have been revealed as a stringent test of the water models. In particular, recently we have determined the phase diagram for different water models and we have found that the performance of the models is quite different.^{34–36} As a consequence, new potentials have been proposed. In this paper we want to perform a detailed analysis of the performance of several popular water models including the recently proposed TIP4P/2005, and to include in the comparison some properties of the solid phases, thus extending the scope of the comparison performed by Guillot.³³ The importance of including solid-phase properties in the test of water models was advocated by Morse and Rice³⁷ and Whalley,³⁸ among others, and Monson suggested that the same should be true for other substances.^{39,40}

It must be recognised that water is flexible and polarizable. That should be taken into account in the next generation of water models.^{41,42} However, it is of interest at this stage to analyse how far it is possible to go in the description of real water with simple (rigid, non-polarizable) models. For this reason we will restrict our study to rigid, non-polarizable models. Besides, in case a certain model performs better than others, it would be of interest to understand why is this so since this information can be useful in the development of future models. As commented above, the study of the phase diagram of water can be extremely useful to discriminate among different water models. Thus, in the comparison between water models, we incorporate not only properties of liquid water but also properties of the solid phases of water. The scheme of this paper is as follows. In Section II, the potential models used in this paper are described. In Section III, we present the properties that will be used in the comparison between the different water models. Section IV gives some details of the calculations of this work. Section V presents the results of this paper. Finally, in Section VI, the main conclusions will be discussed.

II. Water potential models

In this work we shall focus on rigid, non-polarizable models of water. All the models we are considering locate the positive charge on the hydrogen atoms and a Lennard-Jones interaction site on the position of the oxygen. What are the differences between them? They differ in three significant aspects:

- The bond geometry. By bond geometry we mean the choice of the OH bond length and H–O–H bond angle of the model.
- The charge distribution. All the models place one positive charge at the hydrogens but differ in the location of the negative charge(s).
- The target properties. By target properties we mean the properties of real water that were used to fit the potential parameters (forcing the model to reproduce the experimental properties).

In this paper we compare the performance of the following potential models: TIP3P,⁴³ TIP4P,⁴³ TIP5P⁴⁴ and TIP4P/2005.³⁶ This selection presents an advantage. All these models exhibit the same bond geometry (the d_{OH} distance and H–O–H angle in all these models are just those of the molecule in the gas phase, namely 0.9572 Å and 104.52° respectively). Therefore, any difference in their performance

is due to the difference in their charge geometry and/or target properties. Let us now present each of these models.

A. TIP3P

TIP3P was proposed by Jorgensen *et al.*⁴³ In the TIP3P model the negative charge is located on the oxygen atom and the positive charge on the hydrogen atoms. The parameters of the model (*i.e.* the values of the Lennard-Jones (LJ) potential parameters σ and ϵ and the value of the charge on the hydrogen atom) were obtained by reproducing the vaporization enthalpy and liquid density of water at ambient conditions. TIP3P is the model used commonly in certain force fields of biological molecules. A model similar in spirit to TIP3P is SPC.⁴⁵ We shall not discuss the SPC model so extensively in this paper, since we want to keep the discussion within TIP n P geometry (by TIP n P geometry we mean that d_{OH} adopts the value 0.9572 Å and the H–O–H angle is 104.52°). In the SPC model the OH bond length is 1 Å and the H–O–H is 109.47° (the tetrahedral value). The parameters of SPC were obtained in the same way as those of TIP3P. Thus TIP3P and SPC are very similar models. Nine distances must be computed to evaluate the energy between two TIP3P (or SPC) water models so their computational cost is proportional to 9.

B. TIP4P

The key feature of this model is that the site carrying the negative charge (usually denoted as the M site) is not located at the oxygen atom but on the H–O–H bisector at a distance of 0.15 Å. This geometry was already proposed in 1933 by Bernal and Fowler.⁴⁶ TIP4P was proposed by Jorgensen *et al.*⁴³ who determined the parameters of the potential in order to also reproduce the vaporization enthalpy and liquid density of liquid water at room temperature. It is fair to say that TIP4P, although quite popular, is probably less often used than TIP3P or SPC/E. The reader may be surprised to learn that the reasons for that are the appearance of a massless site (the M center) and the apparently higher computational cost. To deal with a massless site within a MD package one must either solve the orientational equations of motion for a rigid body (for instance, using quaternions) or using constraints after distributing the force acting on the M center among the rest of the atoms of the system. These options should be incorporated in the MD package and this is not always the case. Also the computational cost of TIP4P is proportional to 16 when no trick is made (due to the presence of four interaction sites) but it can be reduced to 10 by realizing that one must only compute the O–O distance to compute the LJ contribution, plus 9 distances to compute the Coulombic interaction. Thus, for some users TIP4P is not a good choice as a water model either because it is slower than TIP3P in their molecular dynamics package or because the package may have problems in dealing with a massless site. These are methodological rather than scientific reasons but they appear quite often. Some modern codes such as GROMACS⁴⁷ (just to mention one example) solve these two technical aspects quite efficiently.

C. TIP5P

TIP5P is a relatively recent potential: it was proposed in 2000 by Mahoney and Jorgensen.⁴⁴ This model is the modern version of the models used in the seventies (ST2) in which the negative charge was located at the position of the lone-pair electrons.⁴⁸ Thus instead of having one negative charge at the center M, this model has two negative charges at the L centers. Concerning the target properties this model reproduces the vaporization enthalpy and density of water at ambient conditions. This is in common with TIP3P and TIP4P. However, TIP5P incorporates a new target property: the density maximum of liquid water. The existence of a maximum in density at approximately 277 K is one of the fingerprint properties of liquid water.

Obtaining density maxima in constant temperature and constant pressure (NpT) simulations of water models is not difficult from a methodological point of view.^{31,49,50} However, very long runs are required [of the order of several millions of time steps (MD) or cycles (MC)] to determine accurately the location of the density maximum. Thus, it is not surprising that the very first model able to reproduce the density maximum was proposed in 2000 when the computing power allowed an accurate calculation of the temperature and density at the maximum. Since TIP5P consists of five interaction sites, it apparently requires the evaluation of 25 distances. However, using the trick described for TIP4P, it is possible to show that one just requires the evaluation of 17 distances.

D. SPC/E

In this paper we shall focus mainly on TIP n P-like models. However, it is worth introducing SPC/E,⁵¹ considered by many as one of the best water models. SPC/E has the same bond geometry as SPC. Concerning the charge distribution, it locates the negative charge at the oxygen atom, as do SPC and TIP3P. The target properties of SPC/E were the density and the vaporization enthalpy at room temperature. So far everything seems identical to SPC. The key issue is that SPC/E only reproduces the vaporization enthalpy of real water when a polarization energy correction is included. Berendsen *et al.*⁵¹ pointed out that when using non-polarizable models one should include a polarization correction before comparing the vaporization enthalpy of the model to the experimental value. This is because the dipole moment is enhanced in this type of model in order to account approximately for the neglected many-body polarization forces. Thus, when the vaporization enthalpy is calculated one compares the energy of the liquid with that of a gas with the enhanced dipole moment. It is then necessary to correct for the effect of the difference between the dipole moment of the isolated molecule and that of the effective dipole moment used for the condensed phase. The correction term is given by:

$$\frac{E_{\text{pol}}}{N} = \frac{(\mu - \mu_{\text{gas}})^2}{2\alpha_{\text{p}}} \quad (1)$$

where α_{p} is the polarizability of the water molecule, μ_{gas} is the dipole moment of the molecule in the gas phase and μ is the dipole moment of the model. SPC/E reproduces the vaporization enthalpy of water only if the correction given by eqn (1) is used. The introduction of the polarization correction is the essential feature of SPC/E.

E. TIP4P/2005

The TIP4P/2005 was recently proposed by Abacal and Vega³⁶ after evaluating the phase diagram for the TIP4P and SPC/E models of water.^{34,52} It was found that TIP4P provided a much better description of the phase diagram of water than SPC/E. Both models yielded rather low melting points.⁵³ For this reason, it was clear that the TIP4P could be slightly modified to still predict a correct phase diagram but improve the description of the melting point. The TIP4P/2005 has the same bond geometry as the TIP4P family. Also, TIP4P/2005 has the same charge distribution as TIP4P (although the distance from the M site to the oxygen atom is slightly modified). The main difference between TIP4P and TIP4P/2005 comes from the choice of the target properties used to fit the potential parameters. TIP4P/2005 not only uses a larger number of target properties than any of the water models previously proposed but also they represent a wider range of thermodynamic states. As has become traditional, the first of the target properties is the density of water at room temperature and pressure (but in TIP4P/2005 we have also tried to account for the densities of the solid phases). More significantly, TIP4P/2005 incorporated

those target properties used in the successful SPC/E and TIP5P models. As in SPC/E, the polarization correction is included in the calculation of the vaporization enthalpy. Secondly (as in TIP5P) the maximum in the density of liquid water at room pressure (TMD) was used as a target property. Finally, completely new target properties are the melting temperature of the hexagonal ice (Ih) and a satisfactory description of the complex region of the phase diagram involving different ice polymorphs.

In Table 1 the parameters of the models SPC, SPC/E, TIP4P, TIP5P and TIP4P/2005 are shown. The dipole moment and the three values of the traceless quadrupolar tensor are given in Table 2. There, we also present the values of the quadrupole moment Q_T which is defined as $Q_T = (Q_{xx} - Q_{yy})/2$. We have chosen the H–O–H bisector as the z axis, the x axis in the direction of the line joining the hydrogen atoms so that the y axis is perpendicular to the molecular plane. It can be shown that, for models consisting of just three charges, the value of Q_T is independent of the origin (when the z axis is located along the H–O–H bisector).^{54–56} An interesting feature appears in Table 2. Although for most of water models the dipole moment is close to 2.3 Debye, they differ significantly in their values of the quadrupole moment. Notice that neither the dipole nor the quadrupole moment were used as target properties by any of the water models discussed here. Thus the charge distribution determines the aspect of the quadrupolar tensor. One may suspect that, since quadrupolar forces induce a strong orientational dependence, the differences in the quadrupolar tensor between different water models will be manifested significantly

Table 1 Potential parameters of the water potential models. The distance between the oxygen and hydrogen sites is d_{OH} . The angle formed by hydrogen, oxygen and the other hydrogen atom is denoted as H–O–H. The LJ site is located at the oxygen with parameters σ and (ϵ/k_B) . Proton charge q_H . All the models (except TIP5P) place the negative charge in a point M at a distance d_{OM} from the oxygen along the H–O–H bisector. For TIP5P, d_{OL} is the distance between the oxygen and the L sites placed at the lone electron pairs

Model	$d_{OH}/\text{\AA}$	H–O–H/ $^\circ$	$\sigma/\text{\AA}$	$(\epsilon/k_B)/\text{K}$	q_H/e	$d_{OM}/\text{\AA}$	$d_{OL}/\text{\AA}$
SPC	1.0	109.47	3.1656	78.20	0.41	0	—
SPC/E	1.0	109.47	3.1656	78.20	0.423	0	—
TIP3P	0.9572	104.52	3.1506	76.54	0.417	0	—
TIP4P	0.9572	104.52	3.1540	78.02	0.52	0.15	—
TIP4P/2005	0.9572	104.52	3.1589	93.2	0.5564	0.1546	—
TIP5P	0.9572	104.52	3.1200	80.51	0.241	—	0.70

Table 2 Dipole moment and components of the quadrupole moment. Debye units are used for the dipole moment μ while the components of the quadrupole moment are given in \AA^2 . Q_T is defined as $Q_T = (Q_{xx} - Q_{yy})/2$. The center of mass is used as origin, the z axis being that of the H–O–H bisector and the x axis located in the direction of the vector joining the two hydrogen atoms

Model	μ	Q_{xx}	Q_{yy}	Q_{zz}	Q_T	μ/Q_T
SPC	2.274	2.12	−1.82	−0.29	1.969	1.155
SPC/E	2.350	2.19	−1.88	−0.30	2.035	1.155
TIP3P	2.350	1.76	−1.68	−0.08	1.721	1.363
TIP4P	2.177	2.20	−2.09	−0.11	2.147	1.014
TIP4P/2005	2.305	2.36	−2.23	−0.13	2.297	1.004
TIP5P	2.290	1.65	−1.48	−0.17	1.560	1.460
Gas (expt.)	1.850	2.63	−2.50	−0.13	2.565	0.721

in the solid phases where the relative orientation of the molecules is more or less fixed by the structure of the solid. The coupling between dipolar and quadrupolar interactions is well known since some time ago due to early studies about the behavior of hard spheres with dipole and quadrupole moments.⁵⁷ However, the role of the quadrupole in the properties of water has probably been overlooked although there were some clear warnings about its importance.^{58–60}

III. An exam for water models

In 2002 Guillot presented³³ a study of the performance of water models to describe several properties of water. Although this is only six years ago there are several reasons to perform this study once again. At that time TIP5P had just been released. TIP4P/2005 was proposed three years later. In the intervening years a more precise determination of some properties of the water models (surface tension, temperature of maximum density) has been obtained. More importantly, the calculation in recent years of water properties that were almost completely unknown before (as, for instance, predictions for the solid phases of water, the determination of the melting points and the phase diagram calculations) makes a new comparison of the performance of the models interesting. It is necessary to select some properties to establish the comparison. The selected properties should be as many as possible but representative of the different research communities with an interest in water. We will not include properties of the gas phase (second virial coefficients, vapour densities) in the comparison because only a polarizable model can be successful in describing all the phases of water. Non-polarizable models cannot describe the vapour phase and the condensed phases simultaneously. Thus, the models described above fail in describing vapour properties because they ignore the existence of the molecular polarizability.^{61,62} Therefore, here we will focus only on the properties of the condensed phases (liquid and solids). The ten properties of the test will be the following ones:

- 1. Vapour–liquid equilibria (VLE) and critical point.
- 2. Surface tension.
- 3. Densities of the different ice polymorphs.
- 4. Phase diagram calculations.
- 5. Melting temperature and properties at the melting point.
- 6. Maximum in the density of water at room pressure (TMD). Values of the thermal expansion coefficient, α , and the isothermal compressibility, κ_T .
- 7. Structure of water and ice Ih.
- 8. Equation of state at high pressures.
- 9. Self-diffusion coefficient.
- 10. Dielectric constant.

In order to give an assessment of the quality of the predictions we will assign a score to each of properties depending on the predictions of the model. We recognise that any score is rather arbitrary. We do not pretend to give an absolute test but rather to give a qualitative idea of the relative performance of these water models. So we have devised a simple scoring scheme: for each property we shall assign 0 points to the model with the poorest performance, 1 to the second, 2 to the third and 3 points to the model showing the best performance.

IV. Calculation details

In this work we compare the performance of TIP3P, TIP4P, TIP5P and TIP4P/2005. To perform the comparison we shall use data taken from the literature, either from our previous works or from other authors. For the cases where no results are available we have carried out new simulations to determine them. In all the calculations of this work the LJ part of the potential has been truncated and standard long-range corrections are used. Unless stated otherwise all calculations of this work were

obtained by truncating the LJ part of the potential at 8.5 Å. The importance of an adequate treatment of the long-range Coulombic forces when dealing with water simulations has been pointed out in recent studies.^{63–66} In fact, in the case of water, the simple truncation of the Coulombic part of the potential causes a number of artifacts.^{63–66} In our view, for water the simple truncation of the Coulombic part of the potential should be avoided and one should use a technique treating the long-range Coulombic interactions adequately (as, for instance, Ewald sums or reaction field^{67–69}). The Ewald sums are especially adequate for phase diagram calculations since they can be used not only for the fluid phase but also for the solid phase. Because of this, the Ewald summation technique⁶⁹ has been employed in this work for the calculation of the long-range electrostatic forces. NpT and phase diagram calculations were done with our Monte Carlo code. Transport properties were determined by using GROMACS 3.3.⁴⁷ Isotropic NpT simulations were used for the liquid phase (and cubic solids) while anisotropic Monte Carlo simulations (Parrinello–Rahman-like)^{70,71} were used for the solid phases.

Recently, we have computed the phase diagram for the TIP4P model by means of free-energy calculations. For the solid phases, the Einstein crystal methodology proposed by Frenkel and Ladd was used.⁷² Further details about these free-energy calculations can be found elsewhere.⁷³ For the fluid phase, the free energy was computed by switching off the charges of the water model to arrive at a Lennard-Jones model for which the free energy is well known.⁷⁴ The free-energy calculations for the fluid and solid phases lead to the determination of a single coexistence point for each coexistence line. Starting at this coexistence point, the complete coexistence lines were obtained by using Gibbs–Duhem integration.⁷⁵ The Gibbs–Duhem integration (first proposed by Kofke) is just the numerical integration of the Clapeyron equation:

$$\frac{dp}{dT} = \frac{s_{\text{II}} - s_{\text{I}}}{v_{\text{II}} - v_{\text{I}}} = \frac{h_{\text{II}} - h_{\text{I}}}{T(v_{\text{II}} - v_{\text{I}})} \quad (2)$$

where we use lower case for thermodynamic properties per particle, and the two coexistence phases are labelled as I and II respectively. Since the difference in enthalpy and volume between two phases can be easily determined in computer simulations, the equation can be integrated numerically. Therefore, a combination of free-energy calculations and Gibbs–Duhem integration allowed us to determine the phase diagram of the TIP4P model.

In this work we have also computed the phase diagram for the TIP3P and TIP5P models. Instead of using the free-energy route to obtain the initial coexistence point we have used Hamiltonian Gibbs–Duhem integration⁷⁶ which we briefly summarize. Let us introduce a coupling parameter, λ , which transforms a potential model A into a potential model B (by changing λ from zero to one):

$$U(\lambda) = \lambda U_{\text{B}} + (1 - \lambda)U_{\text{A}}. \quad (3)$$

It is then possible to write a generalized Clapeyron equation as

$$\frac{dT}{d\lambda} = \frac{T \left(\langle u_{\text{B}} - u_{\text{A}} \rangle_{N,p,T,\lambda}^{\text{II}} - \langle u_{\text{B}} - u_{\text{A}} \rangle_{N,p,T,\lambda}^{\text{I}} \right)}{h_{\text{II}} - h_{\text{I}}} \quad (4)$$

where u_{B} is the internal energy per molecule when the interaction between particles is described by U_{B} (and a similar definition for u_{A}). If a coexistence point is known for the system with potential A, it is possible to determine the corresponding coexistence point for the system with potential B (by integrating the previous equations changing λ from zero to one). In this way, the task of determining an initial point of the coexistence lines of the phase diagram of system B is considerably simplified. The initial

coexistence properties for the system A (*i.e.* the reference system) must be known. We have used TIP4P as reference system because its coexistence lines are now well known.^{34,52} The phase diagram for TIP3P and TIP5P reported in this work has been obtained by means of the Hamiltonian Gibbs–Duhem integration starting from the known coexistence points of the TIP4P model. Again, the rest of the coexistence lines have been calculating using the usual Gibbs–Duhem [eqn (2)] integration.

V. Results

1. Vapour–liquid equilibria (VLE) and critical point

The vapour–liquid equilibria of TIP4P and TIP5P have been reported by Nezbeda *et al.*^{64,77,78} Besides, we have recently calculated the VLE of TIP4P/2005.⁷⁹ However, predictions of the vapour–liquid equilibria for the rigid TIP3P model were not found after a literature search (although it was possible to find results⁸⁰ for a flexible TIP3P model). For this reason we proceeded to evaluate the VLE of the TIP3P model. Firstly, we used Hamiltonian Gibbs–Duhem integration to obtain an initial coexistence point for the TIP3P model at 450 K. As initial reference point, we used the coexistence data reported by Lisal *et al.*⁷⁷ of the TIP4P model at 450 K. The LJ part of the potential was truncated at a distance slightly smaller than half the box length (both for the liquid and for the vapour phase). Once the coexistence point at 450 K was obtained for the TIP3P model, the rest of the coexistence line was obtained from Gibbs–Duhem simulations. The coexistence points are presented in Table 3. The critical properties of all TIP n P models are given in Table 4 and Fig. 1 shows the vapour–liquid equilibria for TIP3P, TIP4P, TIP4P/2005 and TIP5P.

The lowest critical temperature corresponds to that of the TIP5P model followed by that of the TIP3P and TIP4P. TIP4P/2005 provides a critical point in very good agreement with experiment. As it can be seen in Fig. 1, TIP4P/2005 also provides an excellent description of the coexistence densities along the orthobaric curve. The description of the critical pressure is not good for any of the models which suggests that the inclusion of polarizability is probably required to reproduce the

Table 3 Vapour liquid equilibria for the TIP3P model as obtained from the computer simulations of this work

T/K	p/bar	$\rho_{\text{gas}}/\text{g cm}^{-3}$	$\rho_{\text{liquid}}/\text{g cm}^{-3}$
550	81.32	0.074(3)	0.543(8)
545	74.74	0.066(2)	0.561(7)
540	68.64	0.058(2)	0.585(5)
530	57.83	0.043(1)	0.613(5)
520	48.44	0.0350(9)	0.643(7)
510	40.48	0.0278(8)	0.668(4)
500	33.58	0.0224(5)	0.697(4)
490	27.62	0.0183(5)	0.720(4)
470	18.30	0.0112(3)	0.760(5)
450	11.72	0.0070(1)	0.799(3)
425	6.313	0.00375(8)	0.836(3)
400	3.142	0.00187(4)	0.873(2)
375	1.412	0.00088(1)	0.904(2)
350	0.5587	0.000361(6)	0.934(2)
325	0.1890	0.000129(2)	0.959(2)
300	0.05203	0.0000380(4)	0.984(2)
275	0.01101	0.00000827(7)	1.004(2)

Table 4 Critical properties of TIP3P, TIP4P, TIP4P/2005 and TIP5P. Values taken from ref. 77 (TIP4P), ref. 79 (TIP4P/2005), ref. 64 (TIP5P) and this work (TIP3P)

Model	T_c /K	p_c /bar	ρ_c /g cm ⁻³
TIP3P	578	126	0.272
TIP4P	588	149	0.315
TIP4P/2005	640	146	0.31
TIP5P	521	86	0.337
Experiment	647.1	220.64	0.322

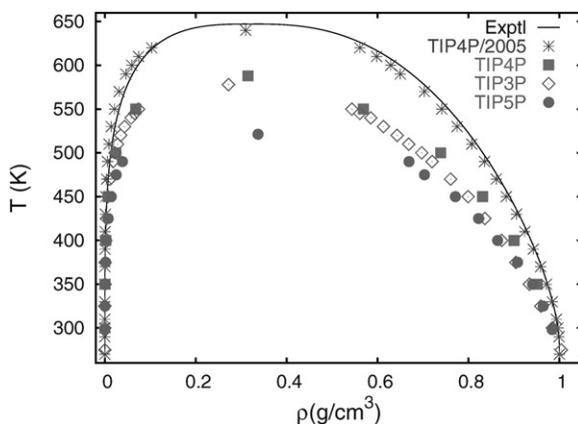


Fig. 1 Vapour–liquid equilibria for TIP3P, TIP4P, TIP5P and TIP4P/2005 models.

experimental value of the critical pressure. Notice that models reproducing the vaporization enthalpy of water without the addition of the polarization term (TIP3P, TIP4P and TIP5P) tend to predict critical temperatures which are too low. The difference between TIP3P and TIP4P is quite small suggesting that three charge models yield a critical point around 580 K when forced to reproduce the vaporization enthalpy. This idea is further reinforced by the critical temperature of SPC, which is of about 590 K.⁸¹ The results for TIP5P indicate that the location of the negative charge at the lone pairs does not solve the problem and this model gives the worst predictions for both the critical temperature and pressure. The success of TIP4P/2005 in estimating the critical point seems to be related to the fact that this model reproduces the vaporization enthalpy only after the inclusion of the polarization correction [as given by eqn (1)]. Further evidence of this is obtained from the fact that SPC/E (which also incorporates the polarization correction) also reproduces the critical temperature of water reasonably well.

The correlation between the critical point and the vaporization enthalpy was first pointed out by Guillot.³³ It is obvious that the value of the vaporization enthalpy is related to the strength of the hydrogen bond in the model. One may try to relate the strength of the hydrogen bond to the magnitude of the dipole and quadrupole moments. The dipole moments of TIP3P, TIP4P, TIP4P/2005 and TIP5P are rather similar but their quadrupole moments differ significantly. TIP5P has the lowest quadrupole moment and TIP4P/2005 has the highest and this is also true for the critical temperatures. However the SPC/E model, which has a relatively low value of the quadrupole moment, yields a satisfactory critical temperature. Obviously the strength of the hydrogen bond depends not only on the multipole moments but also on the parameters of the LJ potential and on the bond geometry. From the

results of the vapour–liquid equilibria, we assign 3 points to TIP4P/2005, 2 points to TIP4P, 1 point to TIP3P and 0 points to TIP5P.

2. Surface tension

The values of the surface tension, γ , for TIP4P and TIP4P/2005 have been reported recently.⁸² For these models the surface tension was obtained using the mechanical route⁸³ (from the normal and perpendicular components of the pressure tensor) and the test area method⁸⁴ (where the Boltzmann factor of a perturbation that changes the interface area but keeps the total volume constant is evaluated). Results obtained from these two methodologies were in good agreement. For TIP5P, results of the surface tension has been reported recently by Chen and Smith.⁸⁵ In this work we have calculated the surface tension for TIP3P using both the mechanical route and the test-area method. Simulations were performed with GROMACS 3.3⁴⁷ for 1024 water molecules with an interface area of about ten by ten molecular diameters. The length of the runs was 2 ns. The LJ part of the potential was truncated at 13 Å. Long-range corrections to the surface tension were included as described in ref. 82. The results for TIP3P are presented in Table 5. The surface tension of TIP3P can be described quite well by the following expression:⁸⁶

$$\gamma = c_1(1 - T/T_c)^{11/9}[1 - c_2(1 - T/T_c)] \quad (5)$$

This expression is used by the IAPWS (International Association for Properties of Water and Steam) to describe the experimental values of the surface tension of water.^{6,87} A fit of the surface tension results for TIP3P furnishes the parameters $T_c = 578.17$ K, $c_1 = 176.42$ mN m⁻¹, $c_2 = 0.57857$. The critical temperature obtained in this way is in good agreement with that obtained from Gibbs–Duhem calculations. Fig. 2 shows the surface tension for TIP3P, TIP4P, TIP4P/2005 and TIP5P. The lowest values of the surface tension correspond to the TIP5P model followed by TIP3P and TIP4P. Again, models reproducing the vaporization enthalpy of water give rather low values of the surface tension. This is consistent with the lower critical temperature of these models. It seems that the TIP4P charge distribution provides a slightly higher value of the surface tension when compared to TIP3P and TIP5P. The predictions of the surface tension of the TIP4P/2005 are in excellent agreement with experiment.^{82,88} How to explain the performance of the different models? Since the surface tension of SPC is similar to that of TIP3P, and that of

Table 5 Surface tension (in mN m⁻¹) for the TIP3P model of water at different temperatures as obtained from computer simulation. ρ_l and ρ_v are the densities (in g cm⁻³) of the liquid and vapour phases at coexistence. \bar{p}_N and \bar{p}_T are the macroscopic values of the normal and tangential components of the pressure tensor (in bar units). l is the thickness of the vapour–liquid interface (in Å). γ_v^* and γ_{ta}^* are the values of the surface tension obtained from the virial route and the test-area method respectively, without including long-range corrections. γ_v and γ_{ta} are the corresponding values of the surface tension, but including long-range corrections which correct for the truncation of the LJ part of the potential at $r_c = 13$ Å (see ref. 82 for details). The values of the surface tension as estimated from this work (γ_{sim}) correspond to the arithmetic average $(\gamma_v + \gamma_{ta})/2$. γ_{exp} are the experimental values of the surface tension

T/K	ρ_l	ρ_v	\bar{p}_N	\bar{p}_T	γ_v^*	γ_{ta}^*	l	γ_v	γ_{ta}	γ_{sim}	γ_{exp}
300	0.980	0.000024	-0.11	-98.44	49.2	49.8	3.87	52.4	52.2	52.3(2.2)	71.73
350	0.930	0.00035	0.22	-80.63	40.4	40.7	4.91	43.3	43.1	43.2(2.0)	63.22
400	0.867	0.0018	2.86	-61.64	32.3	32.9	6.12	34.7	34.5	34.6(1.8)	53.33
450	0.790	0.0069	11.95	-33.81	22.9	23.3	7.82	24.8	24.6	24.7(1.5)	42.88
500	0.689	0.025	33.01	7.61	12.7	12.0	11.53	13.9	13.8	13.9(1.8)	31.61

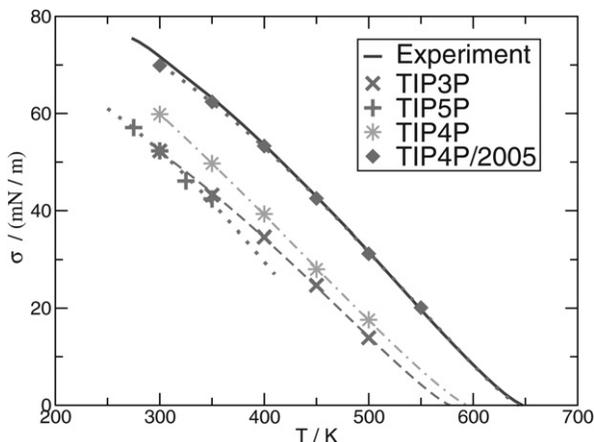


Fig. 2 Surface tension for different water models.

SPC/E is similar to that of TIP4P/2005 (although the predictions of TIP4P/2005 are even better^{82,89} than those of SPC/E), the use of the polarization correction for the vaporization enthalpy seems to be responsible for the improvement of TIP4P/2005 with respect to the TIP3P, TIP4P and TIP5P models. Thus, the use of the polarization correction of Berendsen *et al.*⁵¹ seems to be a prerequisite to obtain models with a good description of the surface tension of water (in non-polarizable models). From the results for the surface tension, we give 3 points to TIP4P/2005, 2 points to TIP4P, 1 point to TIP3P and 0 points to TIP5P. Not surprisingly, the scores of the models are identical to those obtained for the vapour–liquid equilibria.

3. Densities of the different ice polymorphs

In the book *Physics of Ice*,⁴ Petrenko and Whitworth reported the density for several solid phases of water at a certain thermodynamic state. These states are used often to test the performance of water models.^{34,36,90} Simulation results^{34–36,91} indicate that TIP5P overestimates the density of the ices by about seven per cent whereas TIP4P overestimates the densities by less than three per cent and TIP4P/2005 gives an error of less than one per cent. The failure of TIP5P is probably a consequence of a too short distance between the oxygens when the hydrogen bond is formed.⁹² This might also be related to the fact that the negative charge is too far away from the oxygens in TIP5P. In this work we have obtained the predictions for the TIP3P and SPC models which have not been reported yet. We have carried out NpT simulations with anisotropic scaling. For the initial configurations we used the structural data obtained from diffraction experiments. This is all that is needed for ices in which the protons are ordered (II, IX, XI, VIII, XIII, XIV). For ices with proton disorder the oxygens were located using crystallographic information and a proton-disordered configuration (with no net dipole moment and satisfying the Bernal–Fowler rules^{46,93,94}) was generated with the algorithm proposed by Buch *et al.*⁹⁵ Notice that, although we use experimental information to generate the initial solid configuration, the system can relax since we are using the anisotropic NpT scaling in the simulations.

The ice densities for the TIP3P and SPC models are given in Table 6. SPC yields errors of about 2.2%. In general all solid phases were mechanically stable with the SPC model, the only exception being ice XII which melted spontaneously at the simulated temperature. The situation is much worse for the TIP3P model for which several of the solid phases melted spontaneously (in particular ice Ih, III, V and XII). As will be discussed later, this is related to the extremely low melting points of solid

Table 6 Densities and residual internal energies of the different ice phases from NpT simulations for TIP3P and SPC. The experimental data of ices are taken from ref. 4, except those for ice VII (ref. 119) and ice II (ref. 98). The numbers in parenthesis correspond to the cases where the ices are not mechanically stable and melt into liquid water (the reported densities and internal energies then correspond to those of the liquid)

Phase	T/K	p/bar	$\rho/\text{g cm}^{-3}$			$U/\text{kcal mol}^{-1}$	
			Exptl	SPC	TIP3P	SPC	TIP3P
Liquid	300	1	0.996	0.975	0.982	-9.96	-9.66
Ih	250	0	0.920	0.923	(1.021)	-11.72	(-10.23)
Ic	78	0	0.931	0.951	0.959	-13.04	-12.49
II	123	0	1.190	1.219	1.219	-12.94	-12.66
III	250	2800	1.165	1.150	(1.130)	-11.32	(-10.34)
IV	110	0	1.272	1.298	1.286	-12.23	-11.75
V	223	5300	1.283	1.270	(1.226)	-11.60	(-10.73)
VI	225	11000	1.373	1.379	1.366	-11.47	-10.91
VII	300	100000	1.880	1.809	1.826	-8.46	-8.16
VIII	10	24000	1.628	1.661	1.683	-11.41	-11.02
IX	165	2800	1.194	1.198	1.194	-12.55	-12.16
XII	260	5000	1.292	(1.216)	(1.183)	(-10.78)	(-10.26)
XI	5	0	0.934	0.967	0.972	-13.54	-13.01
XIII	80	1	1.251	1.282	1.289	-12.86	-12.48
XIV	80	1	1.294	1.33	1.338	-12.65	-12.22

phases for the TIP3P model.⁵³ Table 6 also reports the internal energies for the different crystalline phases of TIP3P and SPC (those for other models can be found elsewhere^{36,96,97}).

Fig. 3 represents the average deviation from experiment for several ice polymorphs. For the experimental density of ice II we are using the value recently reported by Fortes *et al.*,⁹⁸ which evidenced that the value of Kamb⁹⁹ could be distorted by the presence of helium inside the ice II structure (see also the discussion

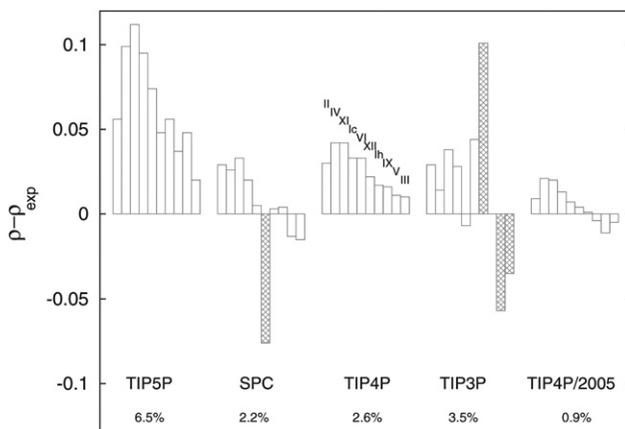


Fig. 3 Deviations in the density predictions for several ice polymorphs at the thermodynamic states reported by Petrenko and Whitworth.⁴ The experimental value of the density for ice II is taken from Fortes *et al.*^{98,121} (instead of the value of Kamb *et al.*^{99,122} used in our previous work). For TIP3P and SPC, the filled rectangles indicate that the corresponding solid phase melts and that the density of the liquid was used to compute the error.

in ref. 97). In fact, the simulation results agree much better with the new reported data of Fortes *et al.*, reinforcing the idea that the value reported by Kamb is probably incorrect.

According to the results of Fig. 3, we assign 3 points to the performance of TIP4P/2005, 2 points to TIP4P, 1 point to TIP5P and 0 points to TIP3P (the low score of TIP3P is due to the fact that several ices melt well below their experimental melting temperatures so that this model is not useful to study the behaviour of the solid phases of water).

4. Phase diagram calculations

The phase diagram of TIP4P, SPC/E and TIP4P/2005 has been determined in previous work.^{34,36,52,100} The phase diagram for TIP3P has not been determined so far. In this work we have used Hamiltonian Gibbs–Duhem integration to compute it and to complete the previous calculations for TIP5P. The results are presented in Fig. 4. The predictions of TIP3P and TIP5P are quite poor. Ice Ih is thermodynamically stable only at negative pressures. The stable phase at the normal melting point for both models is ice II. This surprising result has been confirmed recently by

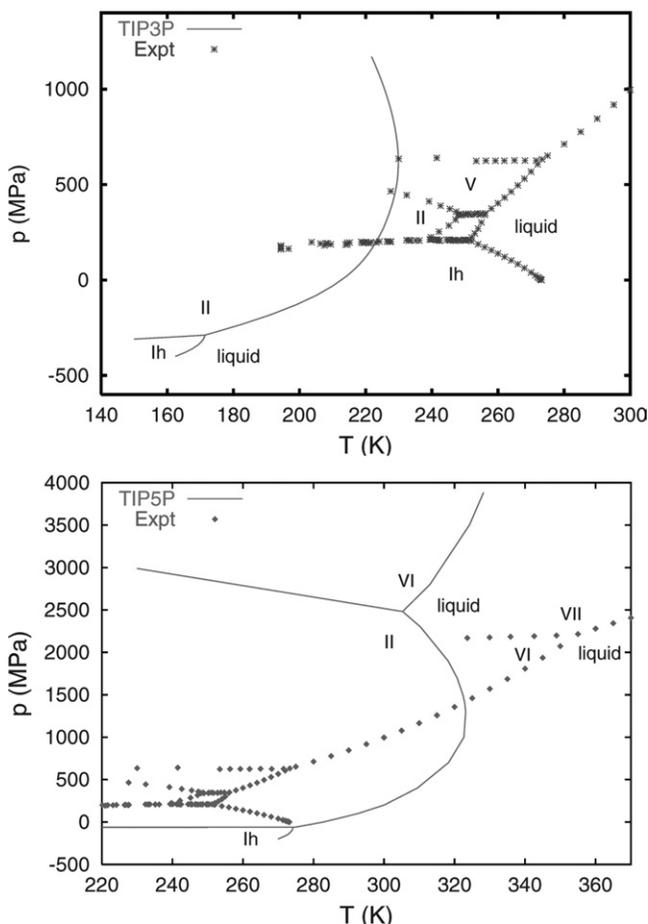


Fig. 4 Phase diagram as obtained in this work for TIP3P and TIP5P. Symbols: experimental phase diagram, lines: computed phase diagram. Top: results for the TIP3P model, bottom: results for the TIP5P model.

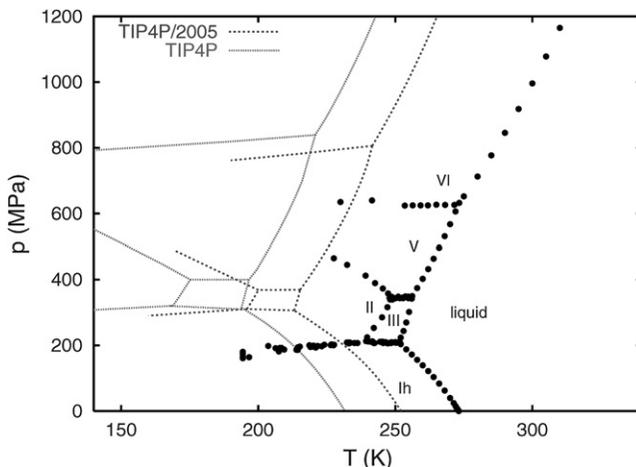


Fig. 5 Phase diagram of TIP4P and TIP4P/2005 models. Symbols: experimental phase diagram, lines: computed phase diagram.

evaluating the properties of ices at zero temperature and pressure.⁹⁶ The performance of TIP4P/2005 is quite good (Fig. 5). The overall performance of TIP4P is also quite good although somewhat shifted to lower temperatures as compared to TIP4P/2005.

What is the origin of the success of TIP4P/2005 and TIP4P? Certainly, it cannot be related to the value of the vaporization enthalpy. This is clear since TIP4P/2005 and TIP4P give good phase diagram predictions and the first uses the polarization correction whereas the second does not. Since the bond geometry of all models is the same, the different performance between them should be related to the differences in the charge distribution. It is not surprising that the solid phases provide information about the orientational dependence of the pair potential in the molecule of water. After all, in the solid phase the molecules adopt certain relative orientations which define the structure of the crystal. Polar forces are strongly dependent on the orientation. Since the dipole moment is similar for TIP3P, TIP4P, TIP4P/2005 and TIP5P, the different predictions found in Fig. 4 and 5 must be related to differences in higher multipolar moments. In fact, as was discussed above, the quadrupole moments for these water models are quite different. We have recently reported that the ratio of the dipole to quadrupole moment seems to play a crucial role in the quality of the phase diagram predicted by the different water models.⁵⁵ As can be seen in Table 2, the ratio μ/Q_T for TIP4P and TIP4P/2005 is about 1 whereas for TIP3P it increases to 1.33. For the TIP5P model the ratio is even larger. In summary, a qualitatively good description of the phase diagram of water requires a reasonable balance between dipolar and quadrupolar forces, and the factor affecting this ratio is just the charge distribution. Not surprisingly, the phase diagram prediction for SPC/E (with a charge distribution similar to that of TIP3P) is also quite poor. Therefore, we assign 3 points to TIP4P/2005, 2 points to TIP4P, 1 point to TIP5P and 0 points to TIP3P.

5. Melting temperature. Properties at melting

Obtaining the melting point of water models is not as obvious as it may appear. The simplest approach (which works fine in the lab⁹) of heating the ice within the simulation box and determining the temperature at which it melts, does not provide the true melting point. In fact, when NpT simulations are performed under periodical boundary conditions, ices usually melt at a temperature about 80–90 K above the

true melting point¹⁰¹ (*i.e.* the temperature at which the chemical potential of the liquid and solid phases are identical). But, in real experiments, ices can not be superheated (at least for a reasonable time). The absence of a free surface is responsible for the superheating of ices in NpT simulations. In fact, when the simulations are performed with a free surface, superheating is suppressed.¹⁰² For this reason the evaluation of the melting point of water models requires special techniques. The melting point of TIP4P was obtained from free-energy calculations of both the fluid and the solid phase. Details of these free-energy calculations have been given recently.⁷³ The melting temperatures of TIP5P, TIP3P and TIP4P/2005 were obtained with Hamiltonian Gibbs–Duhem integration using TIP4P as a reference model. The melting points obtained *via* the free-energy route are in complete agreement with those obtained from direct coexistence simulations^{103–106} where the fluid and solid phases are kept in contact within the simulation box.

We now discuss the melting temperatures of ice Ih for TIP3P, TIP4P, TIP5P, TIP4P/2005 at the standard pressure of 1 bar. It should be mentioned once again that for TIP3P and TIP5P, ice II is more stable than ice Ih at ambient pressure. It is possible to locate the melting point of ice Ih, even though is metastable, provided that it is mechanically stable. For TIP5P the melting point of ice II is about 2 K above that of ice Ih but the melting point of ice II for TIP3P is about 60 K above that of ice Ih. In Table 7, the melting temperature of ice Ih (at 1 bar) and the properties of the solid and the liquid phases at coexistence are given for these models. Concerning the melting temperature, it is as low as 146 K for TIP3P. Thus, TIP3P is probably the poorest model for studying solid phases of water. Since it is possible to simulate ices up to temperatures about 80 K above the melting point, the temperature of 230 K is, roughly speaking, the highest one that can be used to study ice Ih with the TIP3P model. At higher temperatures the TIP3P ice Ih melts. Our estimates for the melting temperature of TIP4P, TIP4P/2005 and TIP5P are approximately 232, 252 and 274 K respectively. The result for TIP4P is in good agreement with the value reported by Gao *et al.*¹⁰⁷ and Koyama *et al.*¹⁰⁸ Another interesting quantity is the ratio of the normal melting temperature to the critical temperature, T_m/T_c . Since the difference between the normal melting temperature and the triple point temperature is only about 0.01 K, this ratio determines the range of existence of the liquid phase for the considered model. Experimentally, $T_m/T_c = 0.42$. The value of the ratio for TIP4P models (TIP4P and TIP4P/2005) is essentially the same, 0.394, but it increases to 0.525 for TIP5P. Thus TIP4P models describe significantly better the experimental range of existence of the liquid phase for water. For TIP3P the ratio is considerably lower (0.25) when the melting temperature of ice Ih (146 K) is considered. But it increases to 0.36 using 210 K as the melting temperature for the stable phase at normal melting for the TIP3P model, which is ice II.

Table 7 Melting properties of ice Ih at $p = 1$ bar for different models. T_m , melting temperatures; ρ_l and ρ_{Ih} , coexistence densities of liquid water and ice; ΔH_m , melting enthalpy; dp/dT , slope of the coexistence curve (between ice Ih and water at the normal melting temperature of the model). We also include for comparison the ratio T_m/T_c . Melting properties are taken from ref. 53 (TIP3P, SPC, SPC/E, TIP4P) and ref. 35 (TIP4P/2005)

Model	TIP3P	SPC	SPC/E	TIP4P	TIP4P/2005	TIP5P	Exptl
T_m/K	146	190	215	232	252	274	273.15
$\rho_l/\text{g cm}^{-3}$	1.017	0.991	1.011	1.002	0.993	0.987	0.999
$\rho_{Ih}/\text{g cm}^{-3}$	0.947	0.934	0.950	0.940	0.921	0.967	0.917
$\Delta H_m/\text{kcal mol}^{-1}$	0.30	0.58	0.74	1.05	1.16	1.75	1.44
$dp/dT/\text{bar K}^{-1}$	-66	-115	-126	-160	-135	-708	-137
T_m/T_c	0.25	0.321	0.337	0.394	0.394	0.525	0.422

Table 7 also presents the coexistence properties (densities at coexistence, slope of the melting curve dp/dT and enthalpy of melting). TIP4P/2005 provides the best estimates of the coexistence densities while TIP5P gives a poor estimate of the density of ice Ih and a completely wrong prediction of the slope dp/dT . This is because, for TIP5P, the densities of ice Ih and of the liquid are quite similar. On the other hand, no model is able to reproduce the melting enthalpy. It is too small (three times lower) for TIP3P. The TIP4P and TIP4P/2005 models also underestimate the melting enthalpy but the errors are much smaller, about 30 and 20% respectively. Finally, TIP5P overestimates the melting enthalpy by approximately 20%.

Let us now try to provide a rational basis for the previous results. For three charge models (TIP3P, TIP4P and TIP4P/2005) there is a clear correlation between the melting temperature of ice Ih and the quadrupole moment of the molecule.^{54,56} Our conclusion is that models locating the negative charge on the oxygen atom have low melting points for ice Ih. Locating the negative charge shifted from the oxygen along the H–O–H bisector increases the melting temperature. The improvement is better if the polarization correction is used in the calculation of the vaporization enthalpy as a target property. When this is done (as in TIP4P/2005) the melting point is about 20 K below the experimental value. This is the closest you can get for the melting point of ice Ih with a three charge model while still describing the vaporization enthalpy with the polarization correction of Berendsen *et al.*⁵¹ The only way of reproducing the experimental melting point of ice Ih within three charge models is to sacrifice the vaporization enthalpy as a target property. In fact, we have developed a model (denoted as TIP4P/Ice)³⁵ which reproduces the melting point of ice Ih but overestimates the vaporization enthalpy. The behaviour of TIP5P is different; it yields a good prediction for the melting temperature in spite of having a low quadrupole moment. Probably the fact that there are two negative charges instead of just one is the responsible for this different behaviour. It is likely that locating the negative charge on the lone-pair electrons enhances the formation of hydrogen bonds in the solid phases provoking an increase in the melting point.

TIP5P reproduces the melting temperature of water. But this is not for free, since the estimate of the coexistence density of ice and of the dp/dT slope then becomes quite poor. Conversely, TIP4P/2005 predicts a rather low melting temperature but it gives quite reasonable estimates for the properties at melting. For this reason, there is no clear winner in this test so we have decided to assign 2.5 points to both TIP5P and TIP4P/2005, 1 point to TIP4P and 0 points to TIP3P.

6. Temperature of maximum density. Thermal coefficients α and κ_T

The density of liquid water for the room pressure isobar as a function of the temperature for TIP3P, SPC and TIP4P with a simple truncation of the Coulombic forces have been reported by Jorgensen and Jenson.¹⁰⁹ Recently, we have also calculated the liquid densities at normal pressure^{36,50} for TIP3P, TIP4P, TIP5P and TIP4P/2005 using Ewald sums to deal with long-range Coulombic forces. Good agreement between our results and those reported by Paschek was found.³¹ Our results are shown in Fig. 6. All models do exhibit a maximum in the density of water along the isobar. For some time it was believed that TIP3P did not exhibit this maximum but it is now clear that the maximum also exists for this model (although located at very low temperatures). In Table 8, the location of the TMD and the values of the thermal expansion coefficient (α) and of the isothermal compressibility (κ_T) at room temperature and pressure are presented. It is clear that the poorest description of the TMD is provided by TIP3P. The behaviour of TIP4P is noticeably better. TIP4P/2005 reproduces nicely the density of water (and its maximum) for all the temperatures along the room pressure isobar. We have shown recently⁵⁰ that—for three charge models like TIP3P, TIP4P and TIP4P/2005—the difference between the TMD and the melting temperature of ice is around 25 K (the experimental difference is 4 K). For this reason, the location of the TMD correlates very well with the

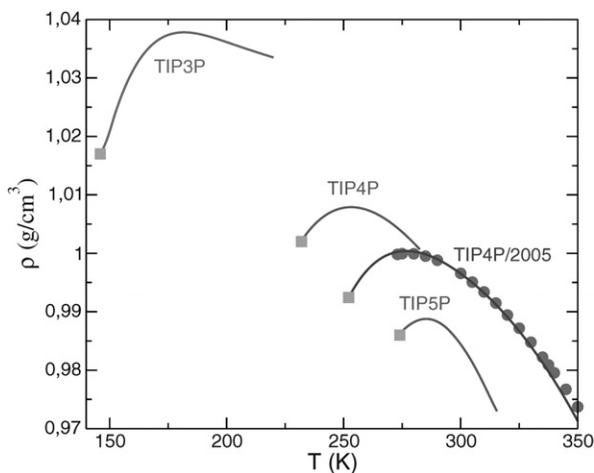


Fig. 6 Maximum in density for several water models at room pressure. Filled circles: experimental results, lines: simulation results. For each model the square represents the location of the melting temperature of the model for ice Ih.

Table 8 Temperature at which the maximum in density occurs T_{TMD} (at room pressure) for different water models. The value of the coefficient of thermal expansion α and of the isothermal compressibility κ_T at room temperature and pressure are also given. The values of α and κ_T for TIP3P, TIP4P and TIP5P as reported in ref. 120. The values for TIP4P/2005 were taken from ref. 36. The value of the maximum in density is as given in ref. 50, except those of the TIP5P that were taken from the original ref. 44

Model	T_{TMD}/K	$10^5 \kappa_T / \text{MPa}^{-1}$	$10^5 \alpha / \text{K}^{-1}$
TIP3P	182	64	92
TIP4P	253	59	44
TIP5P	277	41	63
TIP4P/2005	278	46	28
Experiment	277	45.3	25.6

melting temperature. TIP5P also reproduces the temperature at which the maximum density in water occurs. For the TIP5P the difference between the melting point of ice Ih and the temperature of the maximum in density is about 11 K. In Fig. 6 the densities of TIP5P as obtained from simulations using Ewald summation are presented.

Notice that TIP5P does not reproduce the experimental densities when Ewald summation is used. In the original paper where the TIP5P model was proposed by Mahoney and Jorgensen⁴⁴ the potential was truncated at 9 Å. In these conditions TIP5P reproduces the density of water at the maximum. It has been noticed by other authors that, in general, lower densities are obtained when Ewald sums are implemented than when the electrostatic potential is merely truncated at a given distance. The decrease in density is particularly noticeable in the case of the TIP5P model. For this reason the maximum in density of the TIP5P model occurs at 285 K when Ewald sums are used^{50,64} whereas the maximum takes place at 277 K when the potential is truncated at 9 Å. Fig. 6 shows that for the TIP5P model when the whole normal pressure isobar is considered (not just the maxima), the curvature is not correct. In other words, the dependence of the density on temperature at constant pressure (given by the thermal expansion coefficient α) is not properly predicted by TIP5P

(see Table 8). Importantly, this is also true when the potential is truncated at 9 Å. Therefore, TIP5P does not reproduce α correctly, neither with the potential truncated at 9 Å nor with Ewald sums.

In summary, both TIP4P/2005 and TIP5P reproduce the temperature at which the density maximum occurs. This is by design since the TMD was used as a target property in both models. However, the description of the complete room pressure isobar is much better in the TIP4P/2005 which nicely reproduces the whole curve providing a very good estimate of the coefficient α . Also the estimate of κ_T is better for TIP4P/2005. The excellent description of the densities along the isobar has an interesting consequence. Since the vapour pressure of water is quite small up to relatively high temperatures, orthobaric densities are essentially identical to those obtained from the room pressure isobar. Therefore, a model correctly describing the equation of state along the room pressure isobar will also provide reliable estimates of the orthobaric densities (at least, at temperatures not too close to the critical one). Thus the good description of the ambient pressure isobar of TIP4P/2005 explains in part the good description of the coexistence curve presented previously. Although TIP5P estimates the location of the TMD correctly (when using a cutoff for the electrostatic interactions), it does not yield satisfactory densities for the rest of the room pressure isobar and this explains the poor performance in describing orthobaric coexistence densities. Thus, using the TMD as a target property is a good idea, but it is far better to use the complete room pressure isobar (of course including the maximum) as a target property. For future developments of water potentials we do really recommend using the complete room pressure isobar as a target property. According to the discussion above, we give 3 points to TIP4P/2005, 2 points to TIP5P, 1 point to TIP4P and 0 points to TIP3P.

7. Structure of liquid water and ice

The experimental oxygen–oxygen radial distribution function for liquid water and for ice Ih will be compared to the predictions from the simulations. In Fig. 7 the comparison is made for liquid water. Experimental results are taken from Soper.¹¹⁰ TIP5P provides the best estimate of the radial distribution function. The predictions of TIP4P/2005 are good but the first peak is too high. TIP4P gives quite acceptable predictions but not as good as the previous models. Once again, the discrepancy between the results for TIP3P and experiment is notorious. In Fig. 8 the comparison is made for ice Ih at 77 K and 1 bar. Experimental results are taken from Narten *et al.*¹¹¹ The predictions of TIP4P/2005 are now the best (although it again overestimates the height of the first peak). The results for TIP4P are also very good. Both TIP5P and TIP3P fail in the description of the structure of the solid beyond the first

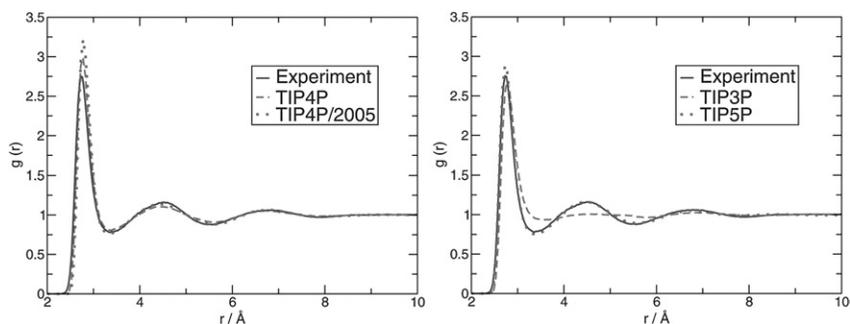


Fig. 7 Oxygen–oxygen radial distribution function for liquid water at $T = 298$ K and $p = 1$ bar. Experimental results were taken from Soper.¹¹⁰ Left: results for TIP4P and TIP4P/2005, right: results for models TIP3P and TIP5P.

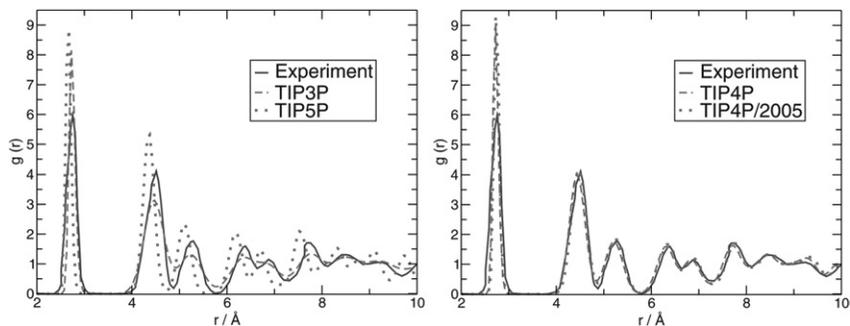


Fig. 8 Oxygen–oxygen radial distribution function for ice Ih at $T = 77$ K and $p = 1$ bar. Experimental results as reported by Narten *et al.*¹¹¹ Left: results for models TIP3P and TIP5P, right: results for TIP4P, TIP4P/2005.

coordination shell. TIP4P/2005 provides good estimates of the radial distribution functions but it overestimates the height of the first peak. It is likely that quantum effects (which could be determined by using path integral simulations) may be significant to understand the amplitude of the first maximum. Indeed, this has been shown to be the case not only for liquid water^{112,113} but also for ice Ih as reported by Kusalik and de la Peña.^{114,115} Further work on this point is probably needed. There is no clear winner concerning structural predictions (TIP5P performs better for water and TIP4P/2005 for ice Ih). For this reason we have decided to give 2.5 points to both TIP5P and TIP4P/2005, one point to TIP4P and zero points to TIP3P.

8. Equation of state of liquid water at high pressures

In a number of geological applications the equation of state (EOS) of water at high temperatures and pressures is needed. Therefore it is of interest to analyze the capacity of these models to predict the behaviour of liquid water at high pressure. Fig. 9 displays the EOS for TIP3P, TIP4P, TIP4P/2005 and TIP5P along the 373 K isotherm for pressures up to 24 000 bar (obtained with 360 water molecules). Experimental results are taken from the EOS of Wagner *et al.*¹¹⁶ and from the experimental measurements of Abramson and Brown.¹¹⁷ TIP4P/2005 provides an

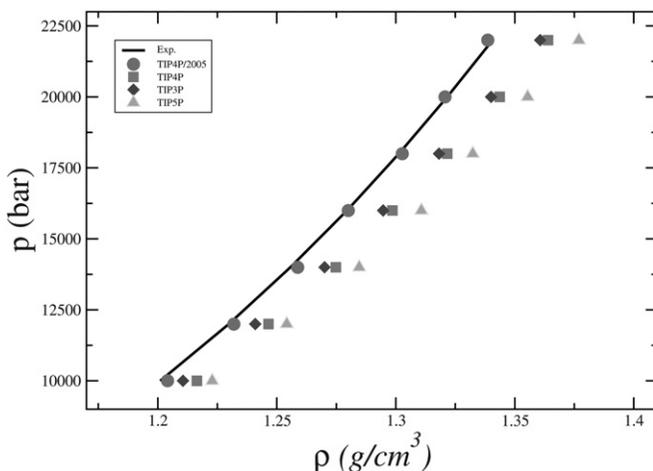


Fig. 9 Equation of state at $T = 373$ K for several water models.

excellent description of the EOS. The differences with experimental data increase for TIP3P followed by TIP4P. The performance of TIP5P is quite poor. We thus assign 3 points to TIP4P/2005, 2 points to TIP3P, 1 point to TIP4P and 0 points to TIP5P.

9. Self-diffusion coefficient

We have computed the self-diffusion coefficient as a function of temperature (at 1 bar) for TIP3P, TIP5P, TIP4P and TIP4P/2005. Simulations were performed with the GROMACS⁴⁷ package and the diffusion coefficients were determined from the slope of the mean square displacement *versus* time (using 360 molecules). A relaxation time of 5 ps was used for the thermostat and for the barostat. Results are presented in Table 9. The diffusion coefficient of TIP3P is too high at all the temperatures investigated. This suggests that the hydrogen bonding for this model is probably too weak. Likely, the weakness of the hydrogen bond is also responsible for the low melting temperature of ice Ih and the loss of structure for the liquid phase beyond the first coordination shell. This may be a big concern in simulation studies of proteins where there must be a competition between intramolecular and intermolecular hydrogen bonds. The diffusion coefficients of TIP4P are closer to experiment but they are still too high, reflecting the fact that using the vaporization enthalpy as a target property leads to highly diffusive water models. TIP5P yields results in agreement with experimental data in the vicinity of 300 K but the departures from experiment greatly increase as the temperature moves away from the ambient one. In fact, at 318 K the result furnished by TIP5P is almost the same as that for TIP4P. Fig. 10 shows that the slope of the line $\log D$ vs. $1/T$ is quite poor (TIP4P

Table 9 Self-diffusion coefficient $10^9 D$ (in $\text{m}^2 \text{s}^{-1}$) for liquid water at 1 bar as a function of temperature

T/K	TIP3P	TIP4P	TIP5P	TIP4P/2005	Experiment
278	3.71	2.08	1.11	1.27	1.313
288	4.34	2.71	1.74	1.57	1.777
298	5.51	3.22	2.77	2.07	2.299
308	6.21	4.12	3.68	2.60	2.919
318	6.32	4.90	4.81	3.07	3.575

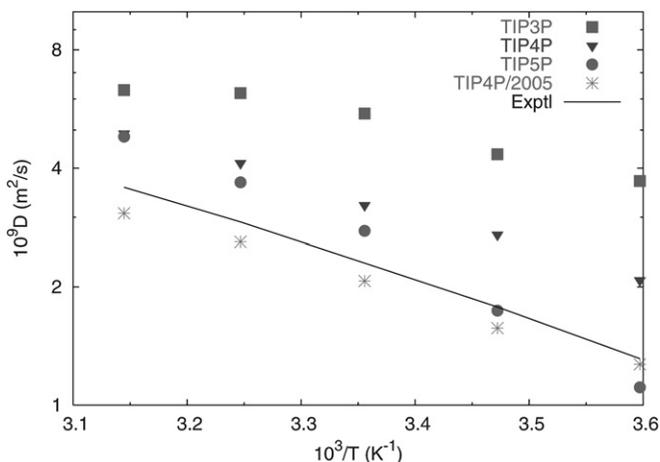


Fig. 10 Logarithmic plot of the self-diffusion coefficients *versus* the inverse of the temperature.

and even TIP3P are superior in this respect). This seems to reflect the overall results of TIP5P: good results at ambient conditions but becoming increasingly bad as one moves away from that point. The best predictions are those of TIP4P/2005. Although a little bit below the experimental values they show the correct trend in its dependence with temperature. Within three charge models, the use of the polarization correction to describe the vaporization enthalpy leads to water models with improved diffusion properties. That was already true for SPC/E (which provides much better diffusion coefficients than SPC) and seems also to be true for TIP4P/2005 (which provides much better estimates of the diffusion coefficients than TIP4P). We therefore give 3 points to TIP4P/2005, 2 points to TIP5P, 1 point to TIP4P and zero points to TIP3P.

10. Dielectric constant

Let us finish by presenting results for the dielectric constant of liquid water at room temperature and pressure. Again, simulations were performed with the package GROMACS⁴⁷ at room temperature and pressure. The simulations lasted 8 ns, and the system consisted of 360 molecules. The value of the dielectric constant is presented in Table 10. TIP5P provides the best estimate of the dielectric constant followed by TIP3P. TIP4P yields the worst value for the dielectric constant. TIP4P/2005 predicts a better dielectric constant than TIP4P but it is still far from the experimental value. It is obvious that the TIP4P charge distribution tends to give low dielectric constants. This is the only property for which the TIP4P charge distribution is in trouble against charge distributions with the negative charge located at the oxygen atom. In fact, the dielectric constants of SPC and SPC/E are better than those of TIP4P and TIP4P/2005, respectively, indicating that locating the charge on the oxygen tends to give better predictions for the dielectric constant. Recently, Rick⁶⁵ has studied the behaviour of the dielectric constant in detail as a function of the dipole and quadrupole moments for different water models. He has shown that a larger dipole increases the value of the dielectric constant whereas a larger quadrupole decreases it. He proposed an equation to correlate the dielectric constant of water models with these multipole moments:

$$\epsilon = -85 + 98\mu - 35.7Q_T \quad (6)$$

where the dipole moment is given in Debye and Q_T in ($\text{D}\text{\AA}$). The dipole moments of all water models are quite similar. However they differ significantly in the value of the quadrupole moment. Thus, the lower value of the dielectric constant for TIP4P models is a direct consequence of the higher quadrupole moment of these type of models. The higher quadrupole moment of TIP4P/2005 was quite good for improving predictions for the melting point and phase diagram. Unfortunately, it also seems responsible for the low dielectric constant of the model.

The dielectric constant is given by the fluctuations of the dipole moment of the sample. It is thus related to the instantaneous values of the polarization of the sample. Non-polarizable models attempt to incorporate (in a mean field way)

Table 10 Computed static dielectric constant ϵ at 298 K and 1 bar

Model	ϵ
TIP3P	94
TIP4P	50
TIP4P/2005	58
TIP5P	91
Experiment	78.4

the effect of the polarizability. Thus, the dipole moments of non-polarizable models are higher than those of the gas phase. It is likely that a property like the dielectric constant, which depends so dramatically on just the dipole moment fluctuations, can hardly be reproduced by an effective potential in which the molecular charge cannot fluctuate. In fact, polarizable models tend to have higher dielectric constants⁴¹ than their non-polarizable counterparts. If this is the case, the good agreement of TIP3P and TIP5P may be somewhat forced. Probably, polarizable versions of TIP3P and TIP5P will tend to give too high dielectric constants whereas the introduction of polarizability will improve the predictions of models based on the TIP4P charge distribution. Further work is required to analyse this issue in more detail since it is difficult at this stage to establish definitive conclusions. Concerning the dielectric constant predictions, we give 3 points to TIP5P, 2 points to TIP3P, 1 point to TIP4P/2005 and 0 points to TIP4P.

VI. Conclusions

Table 11 summarizes the scores obtained by the models for each of the test properties. The final result is that TIP4P/2005 has obtained 27 points, TIP5P 14, TIP4P 13 and TIP3P 6 out of a maximum possible number of 30 points. For most of the properties TIP4P/2005 yielded the best performance. The main exception is the dielectric constant for which TIP4P/2005 yields too low a value. For the second position, TIP5P and TIP4P obtained very similar scores. TIP5P improves the melting point predictions, TMD, dielectric constant and diffusivity with respect to TIP4P, but it is clearly worse in phase diagram predictions, critical point, density of ices and high pressure behaviour. In that respect TIP5P and TIP4P yielded a similar performance and the choice of one or the other potential may depend on the property to be studied. The least satisfactory model, well below any of the others, is TIP3P (see Table 11). Somewhat surprisingly TIP3P is probably the most used model in simulations of biomolecules. In our opinion the only reason to continue using TIP3P is that certain force fields were optimized to be used with TIP3P water. It is not fully obvious whether the force fields must be used with a given water model. Some researchers have challenged this idea.¹¹⁸ In any case, it is clear that new force fields should also be built around better water models.

We have not included the SPC or SPC/E models in the comparison. The performance of SPC is certainly better than that of TIP3P. This is due to the fact that if the negative charge is located on the oxygen, the larger OH bond length of SPC and the tetrahedral bond angle increases the values of the quadrupole moment, and this improves the performance of the model. However, SPC/E yields an overall better performance than SPC. In fact, it improves the prediction of almost all of the

Table 11 Scores obtained by each model for the ten properties considered in this work

Property	TIP3P	TIP4P	TIP4P/2005	TIP5P
1. VLE, T_c	1	2	3	0
2. Surface tension	1	2	3	0
3. ρ ices	0	2	3	1
4. Phase diagram	0	2	3	1
5. T_m melting prop.	0	1	2.5	2.5
6. T_{TMD} , α , κ_T	0	1	3	2
7. Structure	0	1	2.5	2.5
8. EOS (high p)	2	1	3	0
9. D	0	1	3	2
10. ϵ	2	0	1	3
Total	6	13	27	14

properties. The performance of SPC/E, if it had been included in the test, would have been better than that of TIP5P and TIP4P but well below that of TIP4P/2005. The number of points obtained by SPC/E would have been about 21 points (3 for vapour–liquid equilibria, 2 points for surface tension, 2 points for the density of ices, 1 point for the phase diagram, 1 point for the melting properties, 1 point for the TMD, α and κ_T , 2 points for structure predictions, 3 points for the equation of state at high pressures, 3 points for the diffusion coefficient and 3 points for the dielectric constant). Thus, overall SPC/E improves the predictions with respect to TIP4P and TIP5P but is well below the number of points obtained by TIP4P/2005.

Why is the performance of TIP4P/2005 so good in general? TIP4P/2005 is just a TIP4P model with the hydrogen charge augmented from 0.52 e to 0.556 e and with the value of ϵ/k_B increased from 73 to 93 K (the values of σ and d_{OM} are quite similar in both models). It has taken more than twenty years to realize that these two small changes dramatically improve the performance of the model. The steps leading to TIP4P/2005 are basically three. First, the realization of the fact that TIP4P provided a better phase diagram than SPC/E. Secondly, the attempt to improve the prediction of the melting temperature could not be done without accepting the idea of introducing a correction term in the calculation of the vaporization enthalpy. The idea, first introduced by Berendsen *et al.*,⁵¹ enabled them to transform SPC into SPC/E which, in our opinion, is a much better model than SPC. The same could also be useful within the TIP4P geometry, and the final result is TIP4P/2005, but there was an additional refinement. Using the TMD as a target property (as first done by TIP5P) or, even better, fitting the whole room pressure isobar could improve the overall performance. Thus, TIP4P/2005 incorporated this property as a target property. In summary, TIP4P/2005 takes the charge distribution from TIP4P (which yields a reasonable prediction of the phase diagram of water), the use of the correction of Berendsen *et al.* to the vaporization enthalpy from SPC/E, and the use of the TMD as a target property from TIP5P. The resulting model predicts quite nicely the orthobaric densities, critical temperature, surface tension, densities of the different solid phases of water, phase diagram, melting properties (with a reasonable prediction of the melting point about 20 K below the experimental value), TMD, isothermal compressibility, coefficient of thermal expansion and the structure of water and ice. The properties analyzed here cover a temperature range from 120 to 640 K and pressures up to 30 000 bar.

Obviously TIP4P/2005 is not the last word in water potentials and it does have some deficiencies. It fails in the prediction of the vapour properties (vapour pressure, dew densities, critical pressure, second virial coefficient) and in the prediction of the dielectric constant in the liquid phase. However, it really points out clearly the limits that can be achieved by rigid, non-polarizable models. We believe that inclusion of polarizability within a TIP4P/2005-like model (with an adequate fitting of the parameters) would yield further improvement. The extreme sensitivity of phase diagram to the water potential model may help in developing new potential models for water. Now that it is possible to evaluate phase diagrams (both vapour–liquid and fluid–solid) or the TMD on relatively routine basis, it sounds a good idea to extend the incorporation of the phase diagram and the room pressure isobar as target properties in the fitting (and/or checking) of new water models. Although there may be a current of opinion suggesting that polarizable models have not yet improved the performance of non-polarizable models, it is our belief that we have not worked hard enough to refine a reliable polarizable model for water. For the time being, TIP4P/2005 can be considered as a reliable and cheap model of water offering good performance over a wide range of conditions. Since TIP4P/2005 is a minor modification of the model proposed by Bernal and Fowler⁴⁶ in 1933, one may say that we have spend seventy-five years refining their parameters to finally obtain a reliable model of water for the condensed phases.

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